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Exam: Mathematics 2

Hamburg University of Applied Science

Faculty of Engineering & Computer Science, Department of Information and Electrical Engineering Prof. Dr. Robert Heß, January $25^{\rm th}$ 2017, duration: 90 Min.

Permitted aids: up to six A4-pages of personal notes (i.e. single sided sheets)

Result: of 100 points Mark: points.

Problem 1 (15 points)

Solve the following integral: $\int_{-2}^{3} |x^2 - 1| dx$

Problem 2 (15 points)

Derive the Hessian matrix for $f(x, y, z) = xy^2 + y\sin(z) - ze^x$.

Problem 3 (25 points)

For the differential equation $y''' + 6y = 7y' + 4e^x$ find the general solution y(x).

Problem 4 (10 points)

For $y(x) = e^{j(ax+b)}$ with a and b being parameters create the differential equation.

Problem 5 (15 points)



A special unbiased die has eight sides with the numbers 1, 1, 1, 2, 2, 2, 3, 4. Evaluate expectation, variance and standard deviation of this die.

Problem 6 (20 points)

Out of $10\,000$ produced $100\,\mathrm{nF}$ capacitors specified with $10\,\%$ tolerance 139 turn out to be too large and another 139 to be too small in capacitance. Assuming normal distribution what is the standard deviation of capacitance?