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# Exam: Mathematics 2

 $\label{eq:continuous} Hamburg\ University\ of\ Applied\ Science$  Faculty of Engineering & Computer Science, Department of Information and Electrical Engineering Prof. Dr. Robert Heß, July  $7^{\rm th}\ 2016,\ duration:\ 90\ Min.$ 

Permitted aids: up to six A4-pages of personal notes (i.e. single sided sheets)

Result: ...... of 100 points Mark: ..... points.

### Problem 1 (10 points)

Solve the following integral:  $\int x^2 \cos(\frac{1}{2}x^3) dx$ 

#### Problem 2 (15 points)

Draw a contour plot of the function  $f(x,y) = y^2 - x$  for  $x,y \in [-1,1]$  and  $f \in \{-0.5,0,0.5,1\}$ 

#### Problem 3 (25 points)

For the differential equation  $y''' + 2y'' = 3(y' + x^2 - 1)$  find the general solution y(x).

## Problem 4 (10 points)

For  $f(t) = e^{j(\omega t + \varphi)}$  with  $\omega$  and  $\varphi$  being parameters create the differential equation.

# Problem 5 (20 points)

A random variable X has the probability density function  $f(x) = \begin{cases} x/2 & \text{for } 0 \le x < 2 \\ 0 & \text{otherwise} \end{cases}$ . Evaluate expectation, variance and standard deviation.

### Problem 6 (20 points)

As a manufacturer of electronic components you sell  $1\,\mathrm{k}\Omega$  resistors with  $1\,\%$  accuracy. For a large number of resistors you measure an average resistance of  $995\,\Omega$  normal distributed with a standard deviation of  $5\,\Omega$ . Evaluate the failure rate.